

Conservation of Momentum (COp)

- *The momentum of any closed, isolated system does not change.*
- *When objects collide linear momentum is conserved.*
- *Total momentum before the collision equals the total momentum after the collision.*
- *Total energy is also conserved*
 - *Kinetic energy does not have to be conserved.*
 - *Kinetic energy can be transformed to heat.*

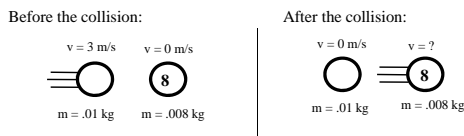
(COp)

- **Types of collisions (remember momentum is conserved):**
 1. **Elastic – kinetic energy is conserved**
 2. **Inelastic – kinetic energy is not conserved**
 3. **Perfectly inelastic – kinetic energy is not conserved and the colliding objects stick together after the collision**

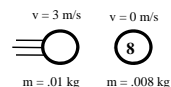
Sample

A 10 gram cue ball is moving at 3 m/s across a pool table toward a stationary 8 ball with a mass of 8 grams. After the collision the cue ball is no longer moving. How fast is the 8 ball traveling?

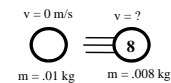
Draw a picture for before and after the collision



Before the collision:



After the collision:



Write a COp equation

Total momentum before equals Total momentum after

$$m_1v_{1i} + m_2v_{2i} = m_1v_{1f} + m_2v_{2f}$$

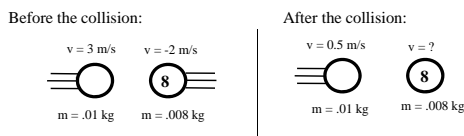
$$(0.01\text{kg})(3\text{m/s}) + (0.008\text{kg})(0\text{m/s}) = (0.01\text{kg})(0\text{m/s}) + (0.008\text{kg})(v)$$

$$v = 3.75\text{m/s}$$

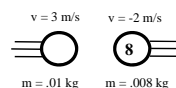
Practice

A 10 gram cue ball is moving at 3 m/s strikes an 8 gram 8 ball moving in the opposite direction at 2 m/s. If, after the collision, the cue ball's velocity is reduced to 0.5 m/s, how fast and in what direction is the 8 ball traveling?

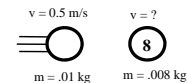
Draw a picture for before and after the collision



Before the collision:



After the collision:



Write a COp equation

Total momentum before equals Total momentum after

$$m_1v_{1i} + m_2v_{2i} = m_1v_{1f} + m_2v_{2f}$$

$$(0.01\text{kg})(3\text{m/s}) + (0.008\text{kg})(-2\text{m/s}) = (0.01\text{kg})(0.5\text{m/s}) + (0.008\text{kg})(v)$$

$$v = 1.125\text{m/s} \quad \text{To the right}$$

Sample

A 5 kg lump of clay moving at 5 m/s collides with a 2 kg stone moving in the **opposite direction**. If the combined clay-stone is brought to rest due to the collision how fast was the stone moving originally?

Draw a picture for before and after the collision

Before the collision:

$v = 5 \text{ m/s}$
 $m = 5 \text{ kg}$

$v = ?$
 $m = 2 \text{ kg}$

After the collision:

$v = 0 \text{ m/s}$
 $m = 7 \text{ kg}$

Sample

Before the collision:

$v = 5 \text{ m/s}$
 $m = 5 \text{ kg}$

$v = ?$
 $m = 2 \text{ kg}$

After the collision:

$v = 0 \text{ m/s}$
 $m = 7 \text{ kg}$

Write a CO_p equation

Total momentum before equals Total momentum after

$$m_1v_{1i} + m_2v_{2i} = (m_1 + m_2)v_f$$

$$(5\text{kg})(5\text{m/s}) + (2\text{kg})v_{2i} = (7\text{kg})(0\text{m/s})$$

$$v_{2i} = -12.5\text{m/s}$$

(CO_p)

Linear momentum is also conserved in "explosions"

You (mass of 65 kg) are standing in a motionless boat (mass = 300 kg). If you jump out of the boat with a velocity of 3 m/s, how fast will the boat be traveling in the opposite direction?

Before the "explosion":

$m = 365 \text{ kg}$
 $v = 0 \text{ m/s}$

After the "explosion":

$m = 65 \text{ kg}$
 $v = -3 \text{ m/s}$

$m = 300 \text{ kg}$
 $v = ? \text{ m/s}$

(CO_p)

Before the "explosion":

$m = 365 \text{ kg}$
 $v = 0 \text{ m/s}$

After the "explosion":

$m = 65 \text{ kg}$
 $v = -3 \text{ m/s}$

$m = 300 \text{ kg}$
 $v = ? \text{ m/s}$

$$(m_1 + m_2)v_i = m_1v_{1f} + m_2v_{2f}$$

$$(365 \text{ kg})(0 \text{ m/s}) = (65 \text{ kg})(-3 \text{ m/s}) + (300 \text{ kg})(v_{2f})$$

$$0.65\text{m/s} = v_{2f}$$

Practice

- A 26 kg cannon ball fired, by Captain Jack Sparrow aboard the Black Pearl (mass 95,750 kg) is moving east at 425 m/s.

➤ What was the velocity of the Black Pearl?

$$(m_1 + m_2)v_i = m_1v_{1f} + m_2v_{2f}$$

$$(26 \text{ kg} + 95,750 \text{ kg})(0 \text{ m/s}) = (26 \text{ kg})(425\text{m/s}) + (95,750 \text{ kg})(v_{2f})$$

$$-0.115\text{m/s} = v_{2f}$$